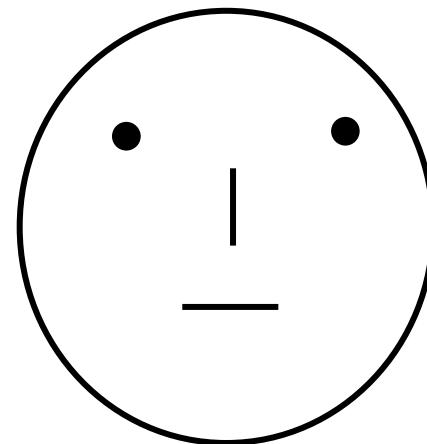


Computergrafik SS 2014

Oliver Vornberger

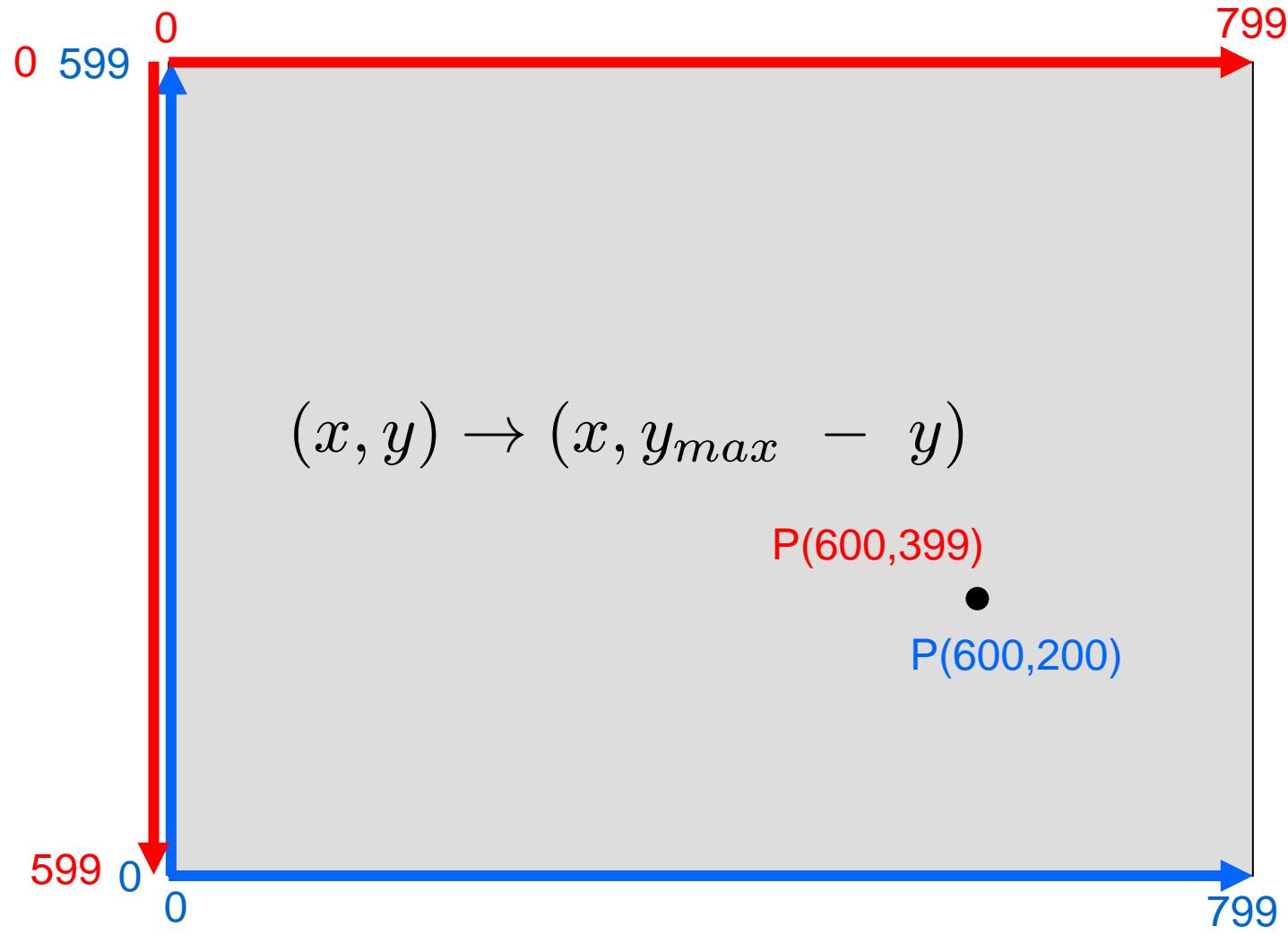
Vorlesung vom 28.04.2014:
Kapitel 3:
2D-Grundlagen

Punkt, Punkt, Komma, Strich, ...

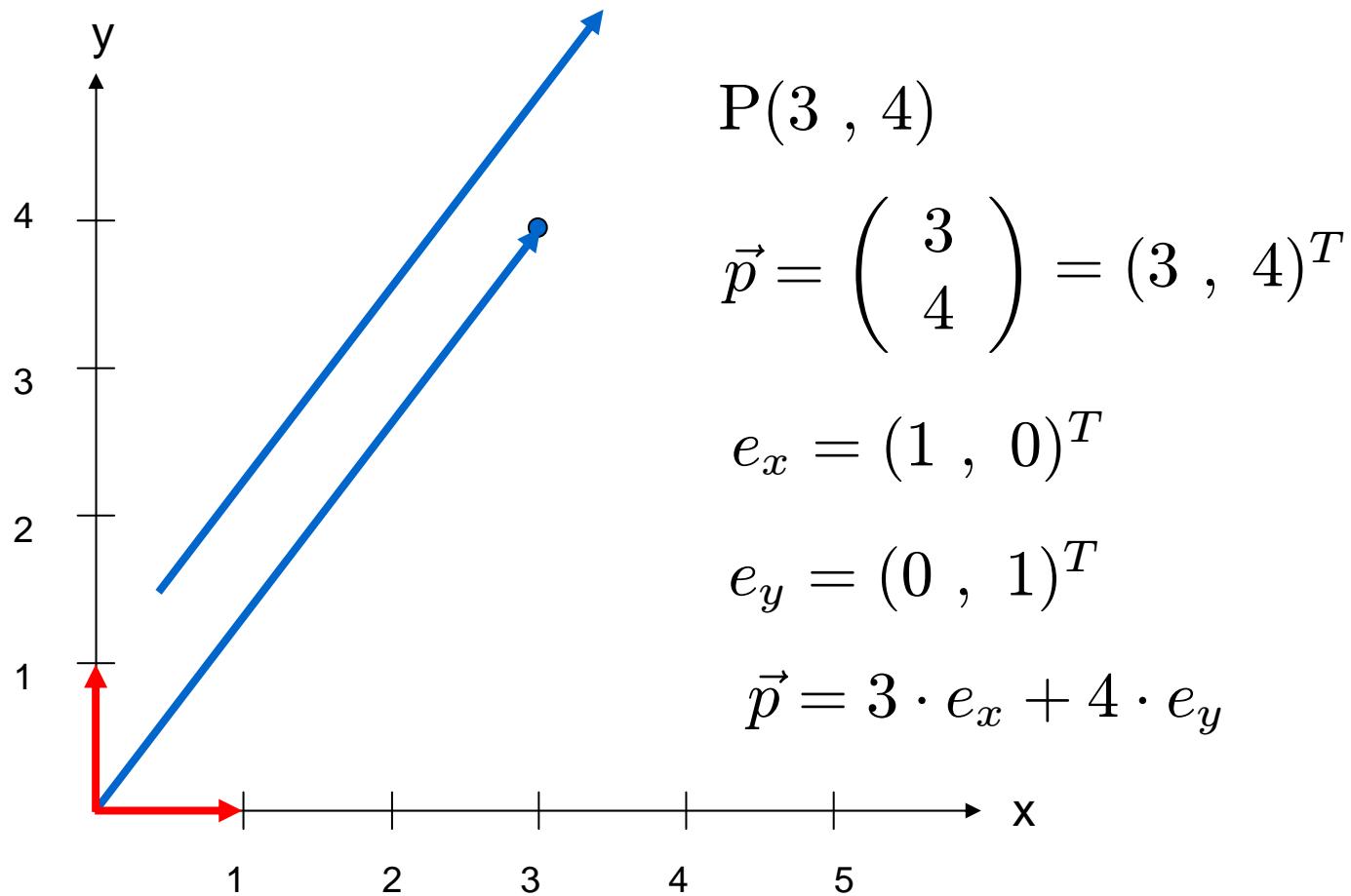


... fertig ist das Mondgesicht !

Koordinatensysteme



Punkt + Vektor

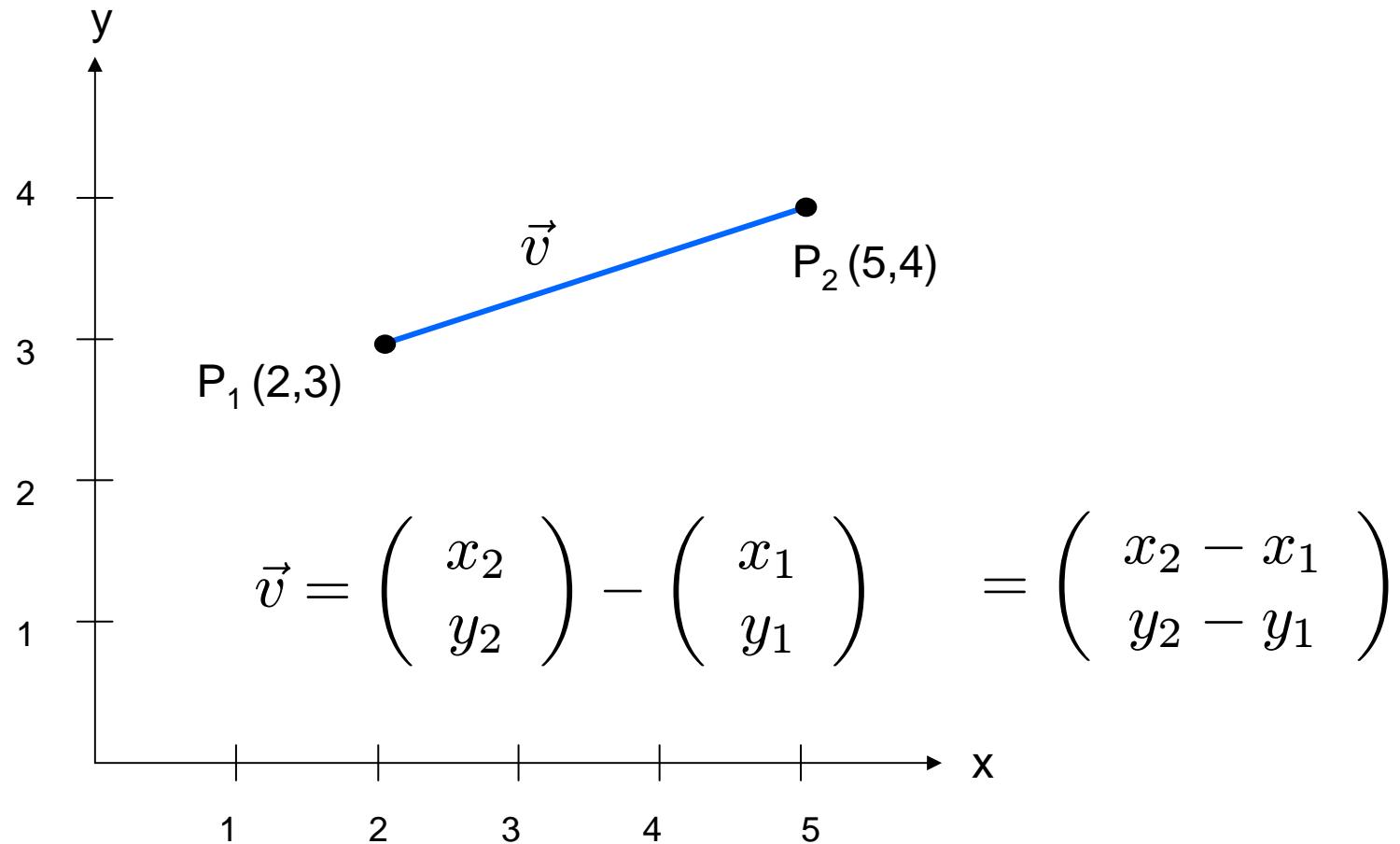


`setPixel(int x, int y)`

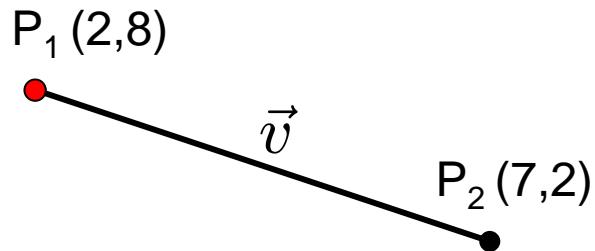
`setPixel(3,4);`

`setPixel((int)(x+0.5),(int)(y+0.5));`

Linie



Parametrisierte Gradengleichung



$$g : \vec{u} = \vec{p}_1 + r \cdot \vec{v}; \quad r \in \mathbb{R}$$
$$l : \vec{u} = \vec{p}_1 + r \cdot \vec{v}; \quad r \in [0; 1]$$

1.0000

$$P = (1 - t) \cdot P_1 + t \cdot P_2$$

$$d = \|\overline{P_1 P_2}\| = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$step = \frac{1}{\sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}}$$

VectorLine

```
int x1,y1,x2,y2,x,y,dx,dy;  
double r, step;  
  
dy = y2-y1;  
dx = x2-x1;  
  
step = 1.0/Math.sqrt(dx*dx+dy*dy);  
for (r=0.0; r <= 1; r=r+step) {  
    x = (int)(x1+r*dx+0.5);  
    y = (int)(y1+r*dy+0.5);  
    setPixel(x,y);  
}
```

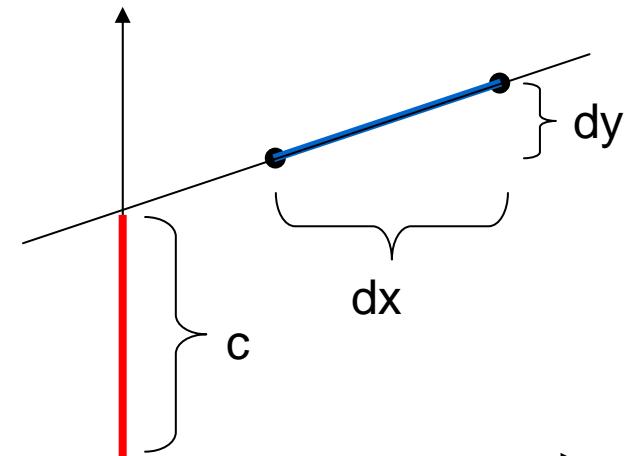
Gradengleichung als Funktion

$$y = f(x) = s \cdot x + c$$

$$s = \frac{y_2 - y_1}{x_2 - x_1}$$

$$\frac{y_1 - c}{x_1 - 0} = \frac{y_2 - y_1}{x_2 - x_1}$$

$$c = \frac{y_1 \cdot x_2 - y_2 \cdot x_1}{x_2 - x_1}$$

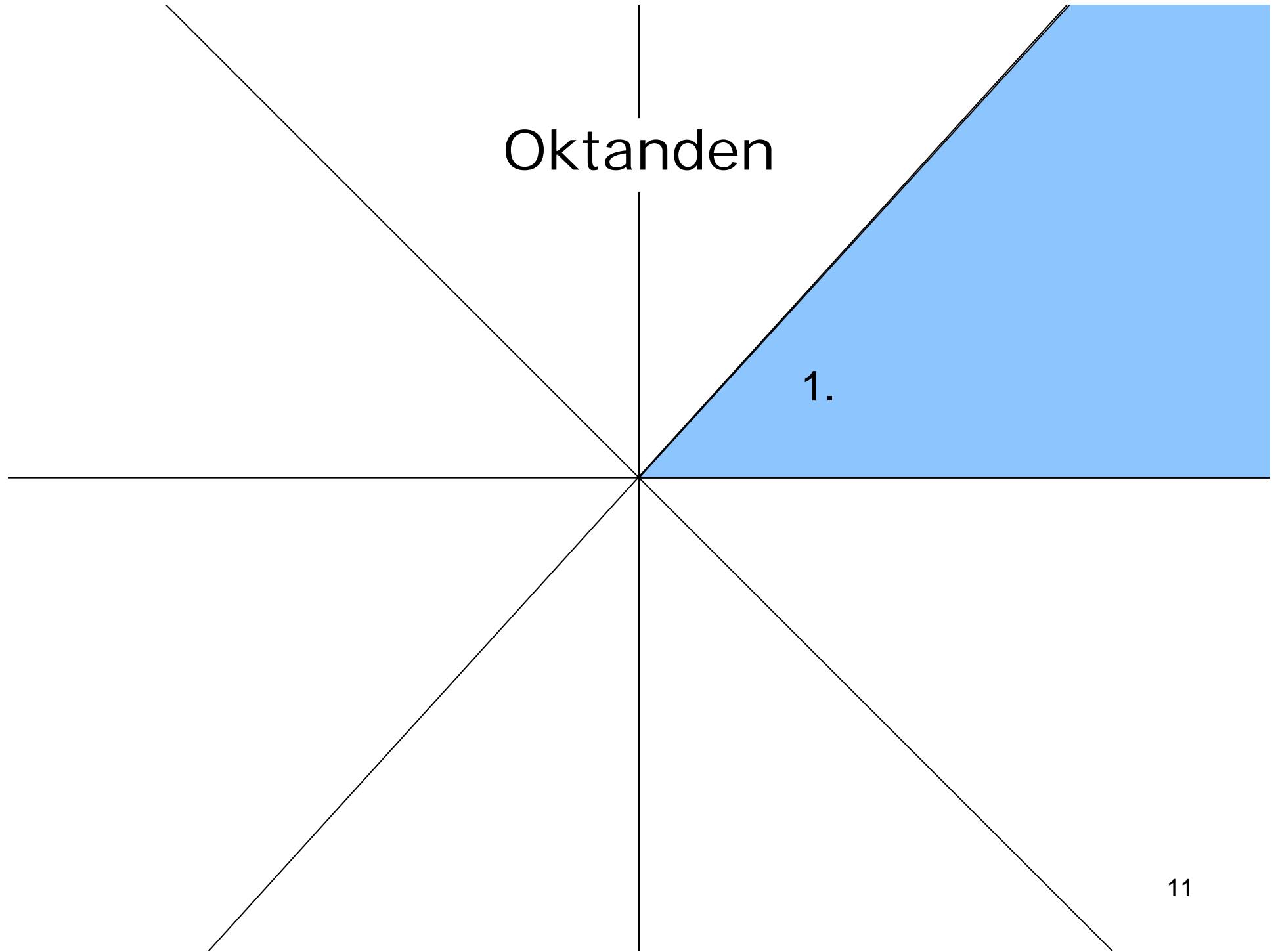


$$y = \frac{y_2 - y_1}{x_2 - x_1} \cdot x + \frac{x_2 \cdot y_1 - x_1 \cdot y_2}{x_2 - x_1}$$

StraightLine

von links nach rechts

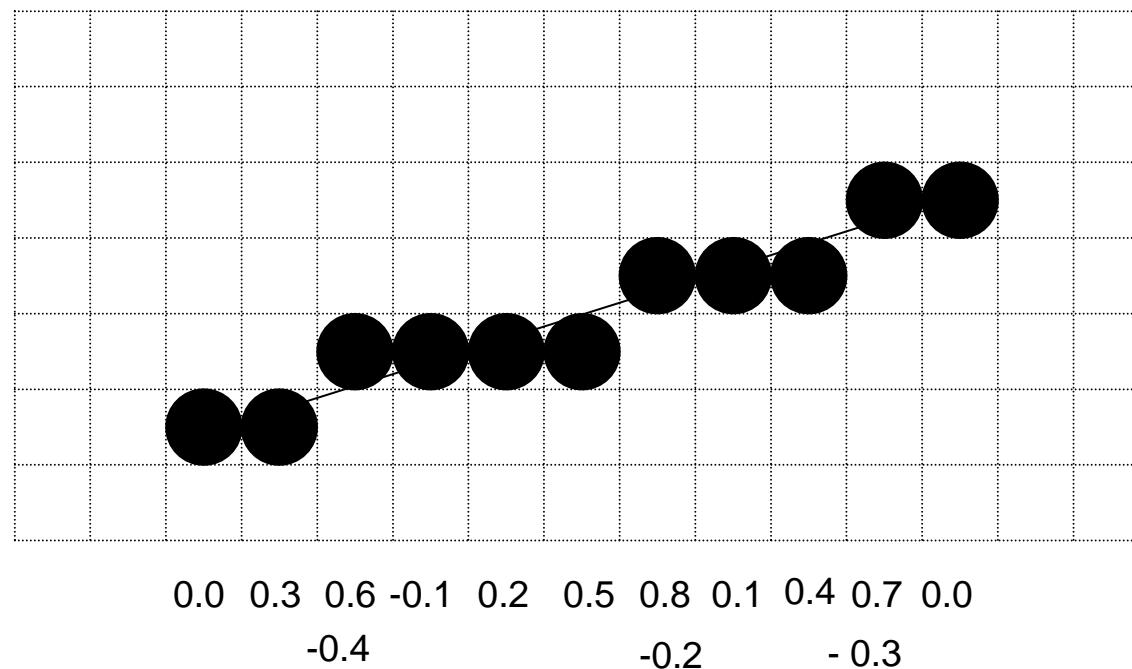
```
s = (double)(y2-y1)/(double)(x2-x1);  
c = (double)(x2*y1-x1*y2)/(double)(x2-x1);  
  
for (x=x1; x <= x2; x++) {  
    y = (int)(s*x+c+0.5);  
    setPixel(x,y);  
}
```



Bresenham

Steigung $s = \Delta y / \Delta x = 3/10 = 0.3$

Fehler $\text{error} = y_{ideal} - y_{real}$



BresenhamLine, die 1.

```
dy = y2-y1; dx = x2-x1;
s = (double)dy/(double)dx;
error = 0.0;
x = x1;
y = y1;
while (x <= x2){
    setPixel(x,y);
    x++;
    error = error + s;
    if (error > 0.5) {
        y++;
        error = error - 1.0;
    }
}
```

BresenhamLine

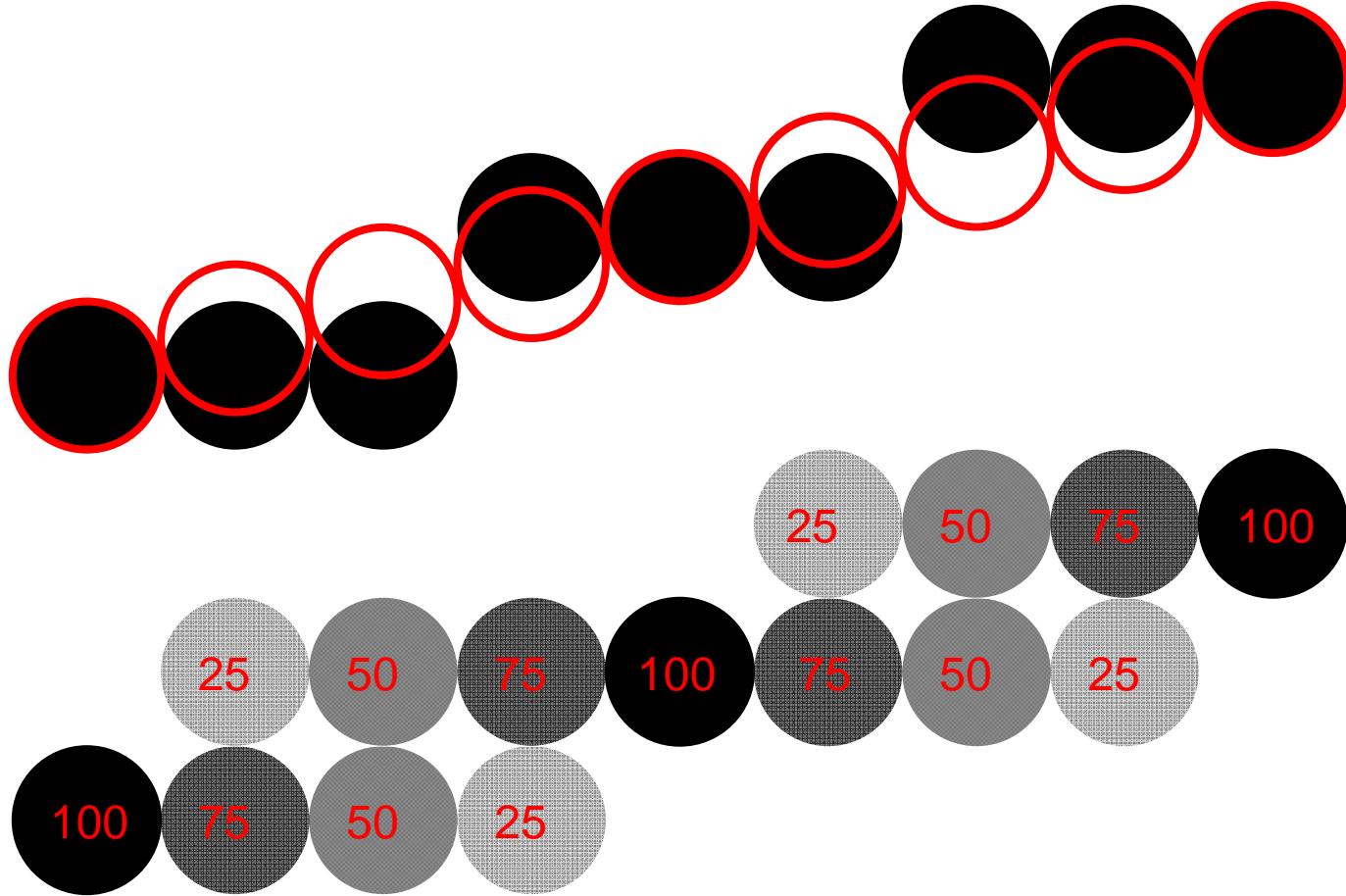
alle 8 Oktanden durch Fallunterscheidung abhandeln:

[~cg/2014/skript/Sources/drawBresenhamLine.jav.html](#)

Java-Applet:

[~cg/2014/skript/Applets/2D-basic/App.html](#)

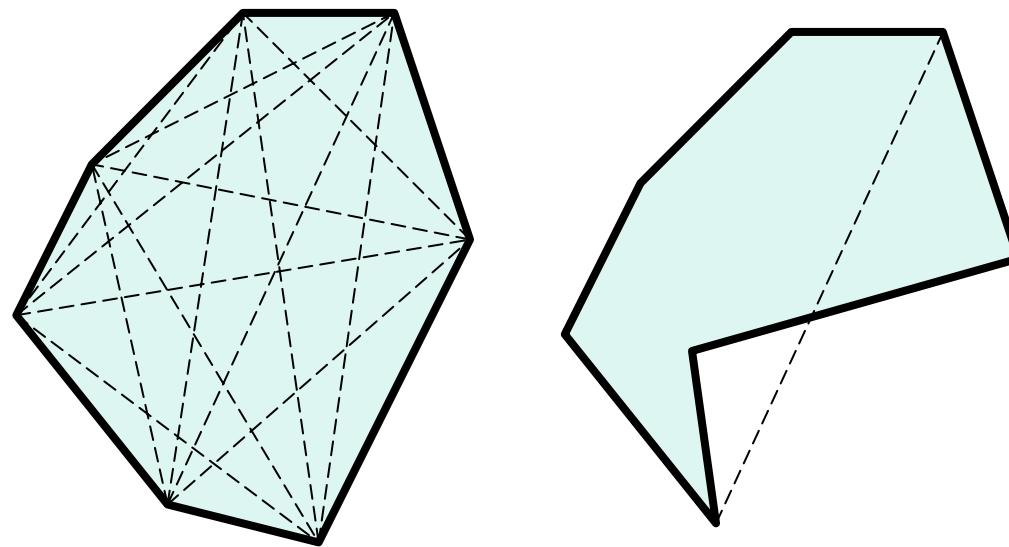
Antialiasing



Antialiasing in Adobe Photoshop



Polygon



konvex

konkav

Punkt versus Gerade

$$\begin{pmatrix} x \\ y \end{pmatrix} = \begin{pmatrix} 2 \\ 3 \end{pmatrix} + r \cdot \begin{pmatrix} 7 - 2 \\ 5 - 3 \end{pmatrix} \quad \vec{u} = \vec{p_1} + r \cdot \vec{v}$$

$$x = 2 + 5r$$

$$y = 3 + 2r$$

$$2x = 4 + 10r$$

$$5y = 15 + 10r$$

$$5y - 2x = 11$$

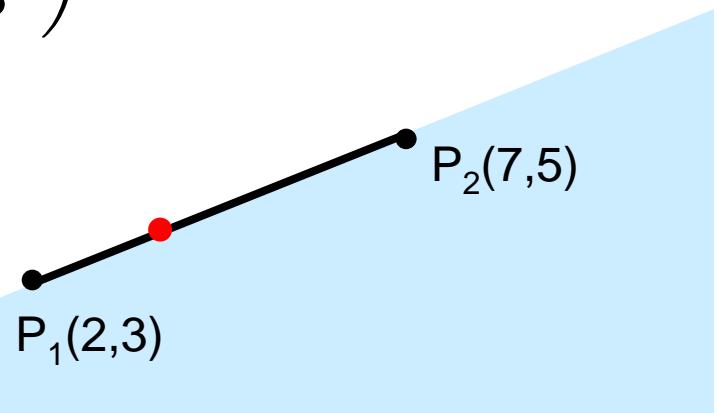
$$5y - 2x - 11 = 0$$

$F(x,y) = 0$ falls P auf der Geraden

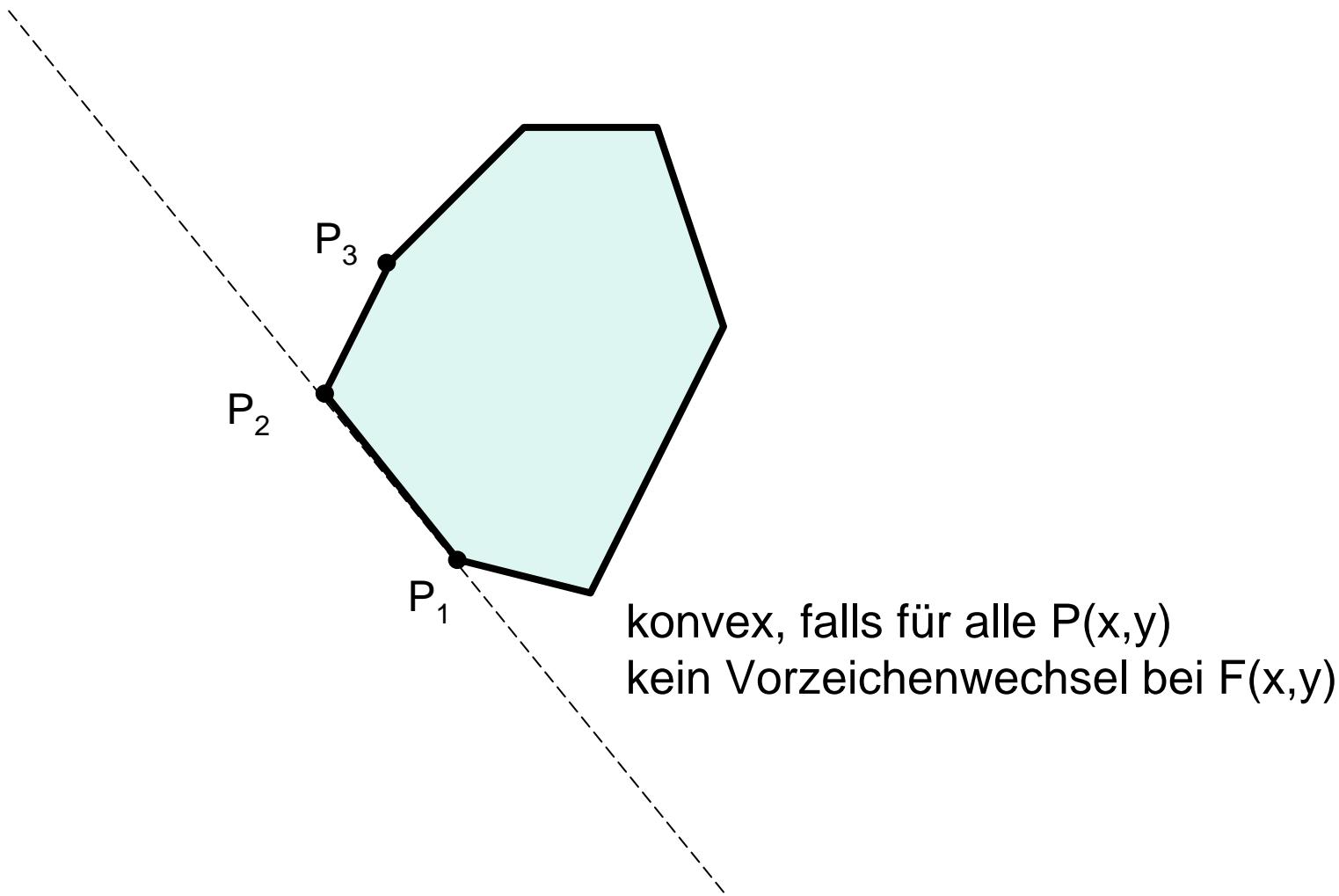
> 0 falls P links von der Geraden

< 0 falls P rechts von der Geraden

$$F(\vec{x}) = (\vec{x} - \vec{p_1}) \cdot \vec{n}$$



Konvexitätstest nach Paul Bourke



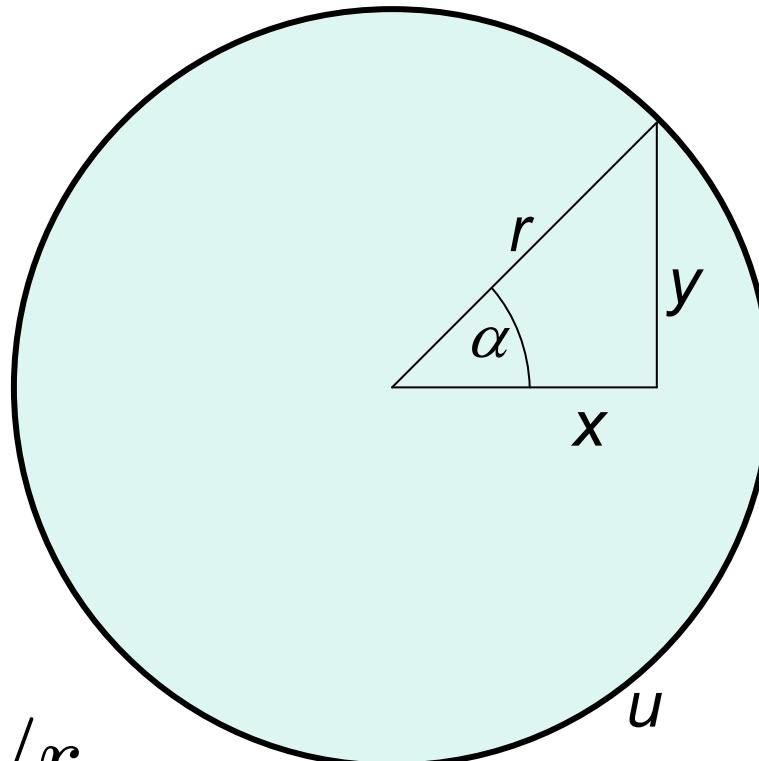
Kreis um $(0,0)$, parametrisiert

$$x = r \cdot \cos(\alpha)$$

$$y = r \cdot \sin(\alpha)$$

$$u = 2 \cdot \pi \cdot r$$

$$step = \frac{2 \cdot \pi}{2 \cdot \pi \cdot r} = 1/r$$



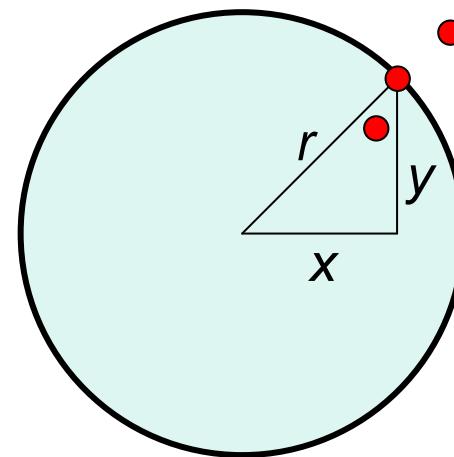
TriCalcCircle

```
double step = 1.0/(double r);
double winkel;

for (winkel = 0.0;
     winkel < 2*Math.PI;
     winkel = winkel+step){

    setPixel((int) r*Math.cos(winkel)+0.5,
             (int) r*Math.sin(winkel)+0.5);
}
```

Punkt versus Kreis

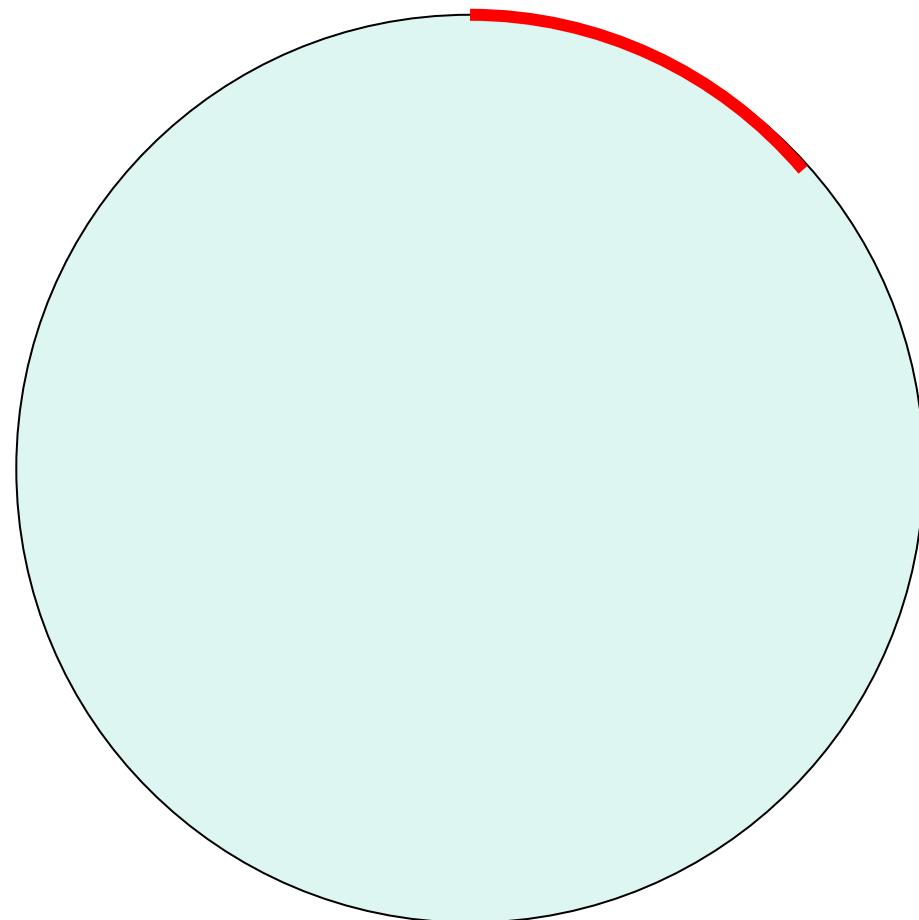


$$x^2 + y^2 = r^2$$

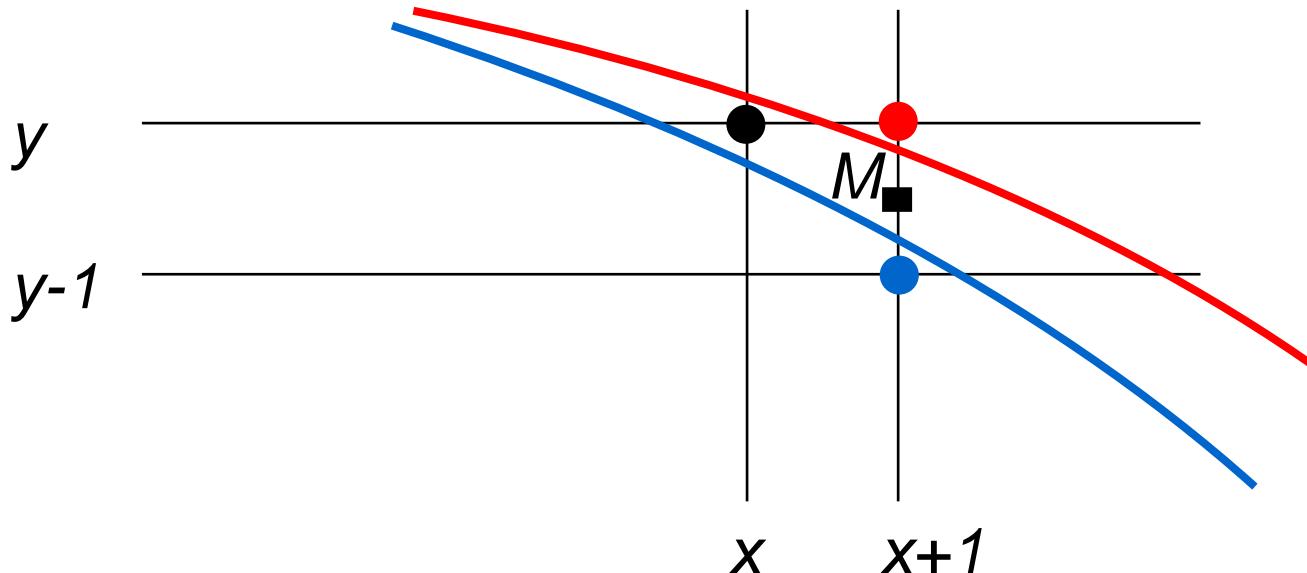
$$F(x,y) = x^2 + y^2 - r^2$$

$F(x,y) = 0$ für (x,y) auf dem Kreis
 < 0 für (x,y) innerhalb des Kreises
 > 0 für (x,y) außerhalb des Kreises

Kreis im 2. Oktanten



Entscheidungsvariable Δ



$$\Delta = F(x+1, y - \frac{1}{2})$$

$\Delta < 0 \Rightarrow M$ liegt innerhalb \Rightarrow wähle $(x+1, y)$

$\Delta \geq 0 \Rightarrow M$ liegt außerhalb \Rightarrow wähle $(x+1, y-1)$

Berechnung von Δ

$$\Delta = F(x+1, y - \frac{1}{2}) = (x+1)^2 + (y - \frac{1}{2})^2 - r^2$$

$$\Delta < 0 \Rightarrow$$

$$\Delta' = F(x+2, y - \frac{1}{2}) = (x+2)^2 + (y - \frac{1}{2})^2 - r^2 =$$

$\Delta + 2x + 3$

$$\Delta \geq 0 \Rightarrow$$

$$\Delta' = F(x+2, y - 3/2) = (x+2)^2 + (y - 3/2)^2 - r^2 =$$

$\Delta + 2x - 2y + 5$

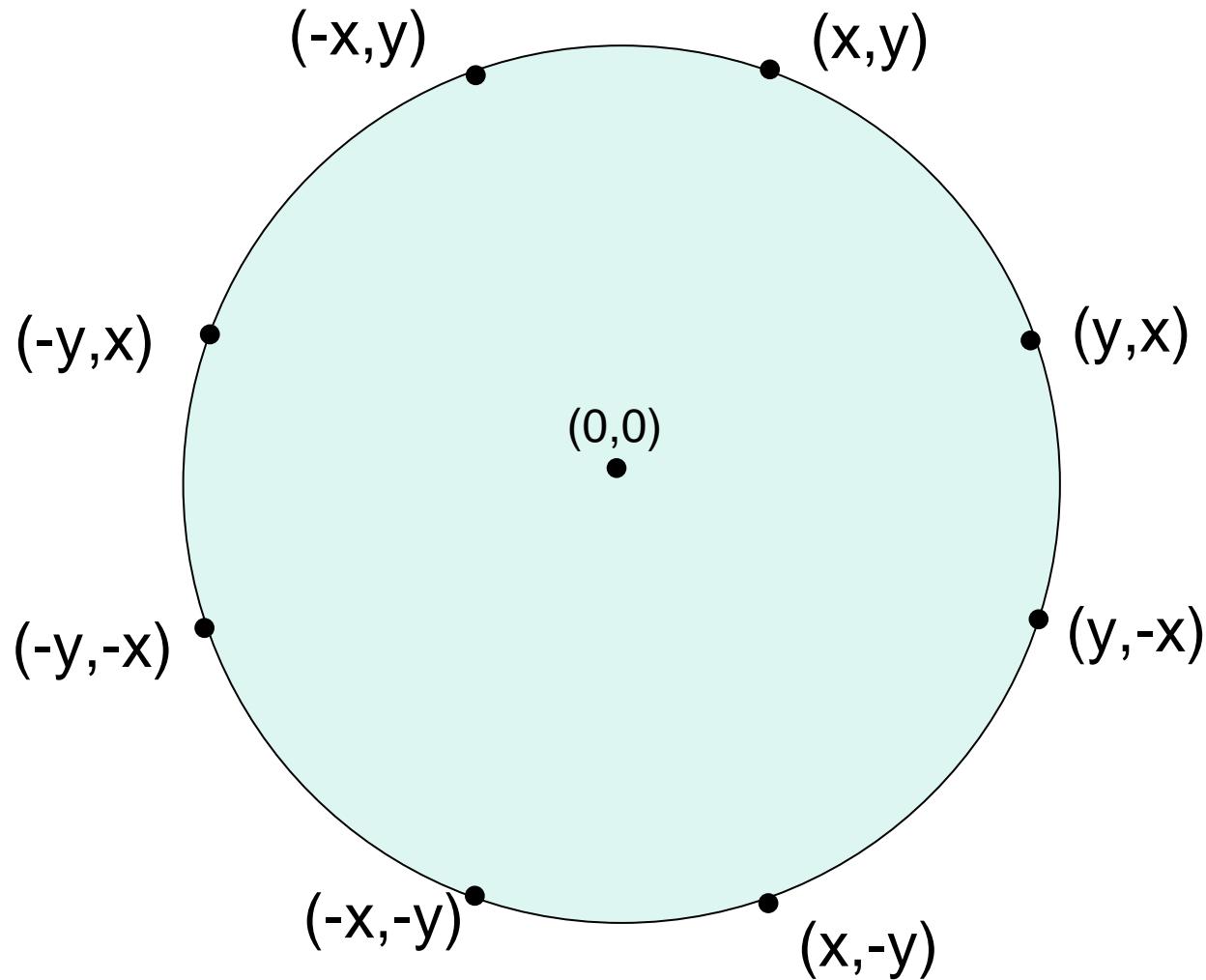
$$\text{Startwert } \Delta = F(1, r - \frac{1}{2}) = 1^2 + (r - \frac{1}{2})^2 - r^2 =$$

$5/4 - r$

BresenhamCircle, die 1.

```
x = 0;  
y = r;  
delta = 5.0/4.0 - r;  
while (y >= x) {  
    setPixel(x,y);  
    if (delta < 0.0) {  
        delta = delta + 2*x + 3.0;  
        x++;  
    } else {  
        delta = delta + 2*x - 2*y + 5.0;  
        x++;  
        y--;  
    }  
}
```

Oktanden-Symmetrie



BresenhamCircle, die 3.

```
x=0; y=r; d=1-r; x=3; dx=3; dxy=-2*r+5;  
while (y>=x){  
    setPixel(+x,+y);  
    setPixel(+y,+x);  
    setPixel(+y,-x);  
    setPixel(+x,-y);  
    setPixel(-x,-y);  
    setPixel(-y,-x);  
    setPixel(-y,+x);  
    setPixel(-x,+y);  
  
    if (d<0) {d=d+dx; dx=dx+2; dxy=dxy+2; x++;}  
    else      {d=d+dxy; dx=dx+2; dxy=dxy+4; x++;  
               y--;}  
}
```

Source: ~cg/2014/skript/Sources/drawBresenhamCircle.java

Java-Applet: ~cg/2014/skript/Applets/2D-basic/App.html

